以 其中,以及1000年3	Group-II	Paper
Math (Science)	(Subjective Type)	Max. Marks:
Time: 2.10 Hours	(Subjective 3,	
	(Part-I)	and the same of th

(Part-I)

2. Write short answers to any Six (6) questions: 12

2. Write short all swells
$$\begin{bmatrix} 8 & 5 \\ 6 & 4 \end{bmatrix} \begin{bmatrix} 2 & -5/2 \\ -4 & 4 \end{bmatrix}$$

Ans Given

$$\begin{bmatrix} 8 & 5 \\ 6 & 4 \end{bmatrix} \begin{bmatrix} 2 & -5/2 \\ -4 & 4 \end{bmatrix}$$

$$= \begin{bmatrix} 8(2) + 5(-4) & 8(\frac{-5}{2}) + 5(4) \\ 6(2) + 4(-4) & 6(\frac{-5}{2}) + 4(4) \end{bmatrix}$$

$$= \begin{bmatrix} 16 - 20 \\ 12 - 16 \\ -4 & 0 \\ -4 & 1 \end{bmatrix} \begin{bmatrix} -20 + 20 \\ -15 + 16 \end{bmatrix}$$

$$= \begin{bmatrix} -4 & 0 \\ -4 & 1 \end{bmatrix}$$

(ii) Define square matrix and give example.

A matrix is called a square matrix if its number of columns. e.g., $A = \begin{bmatrix} 2 & -1 \\ 0 & 3 \end{bmatrix}$

(iii) Use laws of exponents to simplify: $(\frac{8}{125})^{-4/3}$

Ans
$$\left(\frac{8}{125}\right)^{-4/3} = \left(\frac{125}{8}\right)^{4/3}$$

$$= \frac{(125)^{4/3}}{(8)^{4/3}}$$

$$= \frac{(5 \times 5 \times 5)^{4/3}}{(2 \times 2 \times 2)^{4/3}}$$

$$= \frac{(5^3)^{4/3}}{(2^3)^{4/3}}$$

$$=\frac{5^{4}}{2^{4}}$$
$$=\frac{625}{16}$$

(iv) Simplify and write $\left(\frac{1+i}{1-i}\right)^2$ in the form of a + bi.

Ans
$$\left(\frac{1+i}{1-i}\right)^2 = \left[\frac{1+i}{1-i} \times \frac{1+i}{1+i}\right]^2$$

$$= \left[\frac{(1+i)^2}{(1)^2 - (i)^2}\right]^2$$

$$= \left[\frac{1+2i+i^2}{1-(-1)}\right]^2$$

$$= \left[\frac{1+2i+(-1)}{1+1}\right]^2$$

$$= \left[\frac{1+2i-1}{2}\right]^2$$

(v) Find the value of x from the equation: $\log_x 64 = 2$.

Ans Write the above equation in exponential form:

$$x^{2} = 64$$

$$(x)^{2} = (8)^{2}$$

$$\sqrt{x^{2}} = \sqrt{8^{2}}$$

Thus, x = 8

(vi) If $\log 2 = 0.3010$, $\log 3 = 0.4771$, $\log 5 = 0.6990$, then find the value of $\log 30$.

Ans
$$\log 30 = \log (2 \times 3 \times 5)$$

 $\log 30 = \log 2 + \log 3 + \log 5$
 $\log 30 = 0.3010 + 0.4771 + 0.6990$
 $\log 30 = 1.4771$

(viii) Write in the form of a single log
$$1 \log 25 - 2 \log 3$$
 $\log 25 - 2 \log 3 = \log 25 - \log 3^2$ $= \log \frac{25}{3^2}$ (viii) Rationalize the denominator of: $\sqrt{3} - 1$ $\sqrt{3} + 1$ $= \frac{\sqrt{3} - 1}{\sqrt{3} + 1} \times \frac{\sqrt{3} - 1}{\sqrt{3} - 1}$ $= \frac{(\sqrt{3} - 1)^2}{(\sqrt{3})^2 - (1)^2}$ $= \frac{(\sqrt{3})^2 + (1)^2 - 2(\sqrt{3})(1)}{3 - 1}$ $= \frac{3 + 1 - 2\sqrt{3}}{2}$ $= \frac{4 - 2\sqrt{3}}{2}$ $= \frac{4 - 2\sqrt{3}}{2}$ $= (x + 12) - 11(x + 12)$ 3. Write short answers to any Six (6) questions: 18(3³ - 9x² + 8x), 24(x² - 3x + 2) 18(x³ - 9x² + 8x), 24(x² - 3x + 2) 18(x³ - 9x² + 8x) = (2 × 3 × 3) × (x² - 9x + 8) = (2 × 3 × 3) × [x² - x - 8x + 8] = (2 × 2 × 2 × 3) [x² - x - 2x + x - 1] $= (2 × 2 × 2 × 3) [x2 - x - 2x + x - 1]$ $= (2 × 2 × 2 × 3) [x2 - x - 2x + x - 1]$ $= (2 × 2 × 2 × 3) [x2 - x - 2x + x - 1]$

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Now,

$$18(x^3 - 9x^2 + 8x) = 2 \times 3 \times 3 \times x \times (x - 1) \times (x - 8)$$

 $24(x^2 - 3x + 2) = 2 \times 2 \times 2 \times 3 \times (x - 1) \times (x - 2)$
H.C.F = $2 \times 3 \times (x - 1)$
 $= 6(x - 1)$

(ii) Solve the equation and check for extraneous solution: $2\sqrt{t+4}=5$

$$2\sqrt{t+4} = 5$$
$$2(t+4)^{1/2} = 5$$

By squaring both sides:

$$[2(t + 4)^{1/2}]^2 = (5)^2$$

$$4(t + 4)^{1/2 \times 2} = 25$$

$$4(t + 4) = 25$$

$$4t + 16 = 25$$

$$4t = 25 - 16$$

$$4t = 9$$

Check:

$$2\sqrt{t + 4} = 5$$

$$\sqrt{t + 4} = \frac{5}{2}$$
L.H.S = $\sqrt{t + 4}$
= $\sqrt{\frac{9}{4} + 4}$
= $\sqrt{\frac{9 + 16}{4}}$
= $\sqrt{\frac{25}{4}} = \frac{5}{2}$ = R.H.S

iii) Find the solution set:

Ans
$$|3 + 2x| = |6x - 7|$$

 $|3 + 2x| = |6x - 7|$
 $|3 + 2x| = \pm (6x - 7)$

$$3 + 2x = 6x - 7$$
$$3 + 7 = 6x - 2x$$
$$10 = 4x$$
$$\frac{10}{4} = x$$

$$\begin{array}{c} 4 & \times \\ 4 & \times \\ \times & \frac{5}{2} \end{array}$$

Thus, solution set = $\left\{\frac{5}{2}, \frac{1}{2}\right\}$.

$$3 + 2x = -(6x - 7)$$

$$3 + 2x = -6x + 7$$

$$2x + 6x = 7 - 3$$

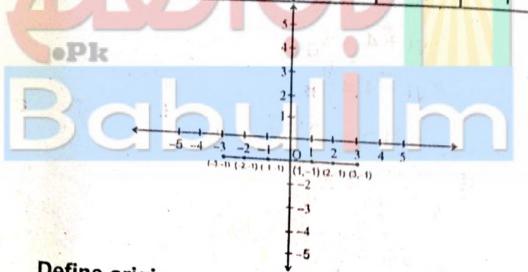
$$8x = 4$$

$$x = \frac{4}{8}$$

(iv) Draw the graph of: y = -1

Ans Table ordered pairs that lie on the graph of y = -1

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x = -3	-2	-1	0	1/	2	Contraction of
y = -1	-1	*···1	-1	1_1	1	and the same of
17 8 1					Contain	-mr



(v) Define origin.

straight lines are drawn. The point where two lines meet

(vi) Find the distance between the following pairs points: A(-8, 1), B(6, 1)

Ans In the above pairs of points:

$$X_1 = -8, X_2 = 6, Y_1 = 1, Y_2 = 1$$

Distance formula:

$$d = \sqrt{|x_2 - x_1|^2 + |y_2 - y_1|^2} = |AB|$$

$$|AB| = \sqrt{[6 - (-8)]^2 + (1 - 1)^2}$$

$$|AB| = \sqrt{(6 + 8)^2 + (0)^2}$$

$$|AB| = \sqrt{14^2}$$

$$|AB| = 14$$

(vii) Find the mid-point of the line segment joining the pairs of points: A(-8, 1), B(6, 1)

Ans A(-8, 1), B(6, 1)
Mid-point =
$$\left(\frac{-8+6}{2}, \frac{1+1}{2}\right)$$

= (-1, 1)

(viii) What is S.A.S postulate?

In any correspondence of two triangles, if two sides and their included angle of one triangle are congruent to the corresponding two sides and their included angle of the other, then the triangles are congruent.

In △ABC ←→ △DEF, shown in the following figures,

$$\overline{AB} \cong \overline{DE}$$
if $AC \cong \overline{DF}$
then $\Delta ABC \cong \Delta DEF$
(S.A.\$ Postulate)

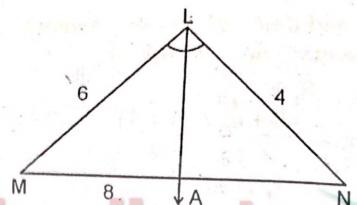
(ix) Define equilateral triangle.

Ans If the length of all the three sides of a triangle are same, then the triangle is called an equilateral triangle.

- 4. Write short answers to any Six (6) questions:
 - (i) Define proportion.

Equality of two ratios is defined as the proportion a: b = c: d; then a, b, c and d are said to be a proportion

(ii) If mLN = 4, $m\overline{ML} = 6$ and $m\overline{MN} = 8$, then find $m\overline{MA}$; $m\overline{AN}$:



Ans Here,

oPk

$$mLM = 6$$
, $mLN = 4$, $mMN = 8$

$$\overline{MMA} = ?$$
 and

$$\overline{MAN} = ?$$

$$\overline{MAN} = x$$

$$\overline{MMA} = 8 - x$$

$$\frac{8-x}{x} = \frac{6}{4}$$

$$4(8-x) = 6x$$

$$32 - 4x = 6x$$

$$32 = 6x + 4x$$

$$32 = 10x$$

$$\frac{32}{10} = x$$

$$x = 3.2$$

$$m\overline{AN} = 3.2$$
and
$$m\overline{MA} = 8 - x$$

$$= 8 - 3.2$$

(iii) Define similar triangles.

Two (or more) triangles are called similar, if they are equiangular and measure of their corresponding sides are proportional. The symbol for similar triangle is (~).

= 4.8

(iv) If 10 cm, 6 cm and 8 cm are the lengths of triangle, verify that sum of two sides of a triangle is greater than the third side.

Let
$$\overrightarrow{mAB} = 10 \text{ cm}$$

$$\overrightarrow{mBC} = 6 \text{ cm}$$

$$\overrightarrow{mCA} = 8 \text{ cm}$$
Now,

$$m\overline{AB} + m\overline{BC} = 10 + 6 = 16 \text{ cm} > m\overline{CA} (= 8 \text{ cm})$$

$$mBC + mCA = 6 + 8 = 14 \text{ cm} > mAB (= 10 \text{ cm})$$

mCA + mAB = 8 + 10 = 18 cm > mBC (= 6 cm)

It is verified that sum of lengths of any two sides of a triangle is greater than the length of the third side.

(v) Verify that the following measures of sides are right angled: a = 9 cm, b = 12 cm, c = 15 cm

Ans
$$a = 9 \text{ cm}$$
, $b = 12 \text{ cm}$, $c = 15 \text{ cm}$
By taking square each

$$(a)^2 = (9)^2$$

 $a^2 = 81$, $(b)^2 = (12)^2$, $(c)^2 = (15)^2$
 $b^2 = 144$, $c^2 = 225$

As we know that:

(vi) If two sides of triangle are 5 cm and 13 cm, then the perpendicular of triangle?

Let, two sides of a triangle:

$$BC = 13$$
 , $\overline{AB} = 5$

Perpendicular of triangle:

As we know that: (Pythagora's Theorem)

$$(\overline{AC})^2 = (\overline{BC})^2 - (\overline{AB})^2$$

 $(\overline{AC})^2 = (13)^2 - (5)^2$
 $(\overline{AC})^2 = 169 - 25$
 $(\overline{AC})^2 = 144$

By taking under root both sides:

$$\sqrt{(\overline{AC})^2} = \sqrt{144}$$

$$\overline{AC} = 12 \text{ cm}$$

- A figure formed by four non-collinear points in plane is called parallelogram. Its characteristics are under:
 - (1) Its equal opposite sides are of equal measure.
 - (2) Its opposite sides are parallel.
 - (3) Measure of none of the angle is 90°.

Area of parallelogram ABCD:

Area = base × altitude

Area = $b \times h$

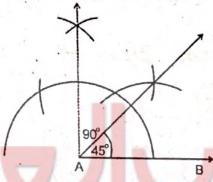
Where

Base =
$$b = \frac{A}{h}$$

Altitude =
$$h = \frac{A}{b}$$

(viii) Bisect the angle of 90°.

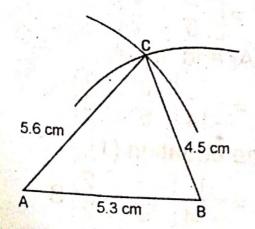




Constructive Procedure:

- (1) Firstly, draw a line segment AB of any measurement.
- (2) At point A, draw a 90° angle.
- (3) Bisect the 90° angle with the help of compass, i.e., 45° angle as shown in the figure.
- (ix) Construct a triangle ABC = mAB = 5.3 cm mBC = 4.5 cm, mCA = 5.6 cm.

Ans



Constructive Procedure:

- Firstly, take a line segment mAB = 5.3 cm. (1)
- Take a point A as centre and draw an arc of 5.6 cm w (2)the help of compass.
- Similarly, take a point B and draw an arc of 4.5 cm. (3)
- Both A and B cut each other at point C. (4)
- By joining these lines, we have constructed AABC. (5)

(Part-II)

NOTE: Attempt any Three (3) questions. But question 9 Compulsory.

Q.5.(a) Solve the system of linear equations using

$$2x - 2y = 4$$
, $-5x - 2y = -10$

$$2x - 2y = 4$$

$$-5x - 2y = -10$$

$$\begin{bmatrix} 2 & -2 \\ -5 & -2 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} 4 \\ -10 \end{bmatrix}$$
Let, $A X = B$

Let,
$$AX = E$$

$$X = A^{-1}B$$

Where,
$$A^{-1} = \frac{1 \text{ Adj. A}}{|A|}$$

$$|A| = \begin{vmatrix} 2 & -2 \\ -5 & -3 \end{vmatrix}$$

$$|A| = (2)(-2) - (-5)(-2)$$

 $|A| = -4 - 10$

$$|A| = -14$$

adj.
$$A = \begin{bmatrix} -2 & 2 \\ 5 & 2 \end{bmatrix}$$

By putting |A| and adj. A

Put A-1 in the equation (1),
$$X = -1 \begin{bmatrix} -2 & 2 \\ 5 & 2 \end{bmatrix}$$

$$X = \frac{1}{-14} \begin{bmatrix} -2 & 2 \\ 5 & 2 \end{bmatrix} B$$

(1)

(1

L

$$= \sqrt{\frac{6^2 \times 5}{5^{(-2)} \times (-3/2)}}$$

$$= \sqrt{\frac{6^2 \times 5}{5^3}}$$

$$= \sqrt{\frac{6^2}{5^3} \cdot 5^{-1}}$$

$$= \sqrt{\frac{6^2}{5^2}}$$

$$= \left(\frac{6^2}{5^2}\right)^{1/2}$$

$$= \frac{6^2 \times 1/2}{5^2 \times 1/2}$$

$$= \frac{6}{5}$$

Q.6.(a) Use logarithm tables to find the value of:

 $\frac{0.7214 \times 20.37}{60.8}$

Ans Let
$$x = \sqrt[3]{\left(\frac{0.7214 \times 20.37}{60.8}\right)}$$

By taking 'log' both sides:

$$\log x = \log \left(\frac{0.7214 \times 20.37}{60.8} \right)^{1/3}$$

$$\log x = \frac{1}{3} \left[\log(0.7214) + \log(20.37) - \log(60.8) \right]$$

$$\log x = \frac{1}{3}[\bar{1}.8582 + 1.3090 - 1.7839]$$

$$\log x = \frac{1}{3} \left[-1 + 0.8582 + 1.3090 - 1.7839 \right]$$

$$\log x = -0.3056$$

$$\log x = -0.2056 - 1 + 1$$

$$\log x = \overline{1}.7944$$

By taking antilog both sides:

$$x = Antilog (1.7944)$$

 $x = 0.6229$ Ans

(b) If $q = \sqrt{5} + 2$, then find the values of $q - \frac{1}{q}$ and $q^2 +$

$$\frac{1}{q^2}.$$
 (4)

Ans Given

$$q = \sqrt{5} + 2$$

$$\frac{1}{q} = \frac{1}{\sqrt{5} + 2}$$

$$= \frac{1}{\sqrt{5} + 2} \times \frac{\sqrt{5} - 2}{\sqrt{5} - 2}$$

$$= \frac{\sqrt{5} - 2}{(\sqrt{5})^2 - (2)^2}$$
(i)
(ii)

$$= \frac{(\sqrt{5})^2 - 2}{5 - 4}$$

$$= \frac{\sqrt{5} - 2}{\sqrt{5} - 2}$$

$$=\frac{\sqrt{5}-2}{1}$$

$$\frac{1}{q} = \sqrt{5} - 2$$

Subtract eq. (i) and (ii)

oPk

$$q - \frac{1}{q} = (\sqrt{5} + 2) - (\sqrt{5} - 2)$$
$$= \sqrt{5} + 2 - \sqrt{5} + 2$$

$$q - \frac{1}{q} = 4$$

By taking square of both sides,

$$\left(q - \frac{1}{q}\right)^2 = (4)$$

$$q^2 + \frac{1}{q^2} - 2(q)(\frac{1}{q}) = 16$$

$$q^2 + \frac{1}{q^2} - 2 = 16$$

$$q^{2} + \frac{1}{q^{2}} = 16 + 2$$

$$q^{2} + \frac{1}{q^{2}} = 18$$

Q.7.(a) Factorize the cubic polynomials by fac

Let, $P(x) = x^3 + x^2 - 10x + 8$ The possible factors of the constant term:

are \pm 1, \pm 2, \pm 4, \pm 8

From factors of the constant:

Let,
$$x = 1$$

 $P(1) = (1)^3 + (1)^2 - 10(1) + 8$
 $= 1 + 1 - 10 + 8$
 $P(1) = 0$

Hence,

x = 1 is a zero of P(x),

As
$$x-a=0$$

 $x-1=0$

So, x - 1 is the 1st factor of P(x). Similarly,

Let x=2

$$P(2) = (2)^3 + (2)^2 - 10(2) + 8$$
$$= 8 + 4 - 20 + 8$$
$$P(2) = 0$$

Hence, x = 2 is a zero of P(x):

$$x-a=0$$

$$x-2=0$$

So, x-2 is the 2^{nd} factor of P(x).

Let
$$x = -4$$

 $P(-4) = (-4)^3 + (-4)^2 - 10(-4) + 8$

$$=-64+64$$

$$P(-4) = 0$$

Hence, x = -4 is a zero of P(x);

As
$$x-a=0$$

$$x - (-4) = 0$$

$$x + 4 = 0$$

So, x + 4 is the 3rd and last factor of P(x), as from the expression, there exists maximum three factor, *i.e.*,

The factors of P(x) are:

$$(x-1)(x-2)(x+4)$$

(b) For what value of k for which following expression will become a perfect square: $x^4 - 4x^3 + 10x^2 - kx + 9$.

Ans

$$x^{2}-2x + 3$$

$$x^{4}-4x^{3} + 10x^{2} - kx + 9$$

$$\pm x^{4}$$

$$2x^{2}-2x$$

$$-4x^{3} + 10x^{2} - kx + 9$$

$$\pm 4x^{3} + 4x^{2}$$

$$2x^{2}-4x + 3$$

$$6x^{2} - kx + 9$$

$$\pm 6x^{2} \mp 12x \pm 9$$

$$-kx + 12x$$

In case of perfect square, remainder must be zero. Thus,

$$-kx + 12x = 0$$

 $x(-k + 12) = 0$
 $-k + 12 = 0$
 $12 = k$
 $k = 12$

Q.8.(a) Solve the equation and check:

$$\sqrt{5x-7}-\sqrt{x+10}=0$$

Ans Given: $\sqrt{5}x - 7 - \sqrt{x + 10} = 0$

$$\sqrt{5x-7} = \sqrt{x+10}$$

By taking square both sides:

$$(\sqrt{5x-7})^2 = (\sqrt{x+10})^2$$
$$5x - 7 = x + 10$$
$$5x - x = 10 + 7$$

$$4x = 17$$

$$x = \frac{17}{4}$$

Check:

Substituting $x = \frac{17}{4}$ in original equation:

$$\frac{\sqrt{5x-7} - \sqrt{x+10}}{\sqrt{5(\frac{17}{4})-7} - \sqrt{\frac{17}{4}+10}} = 0$$

$$\frac{\sqrt{5x-7} - \sqrt{x+10}}{\sqrt{4}+10} = 0$$

$$\sqrt{\frac{85 - 28}{4}} - \sqrt{\frac{17 + 40}{4}} = 0$$

$$\sqrt{\frac{57}{4}} - \sqrt{\frac{57}{4}} = 0$$

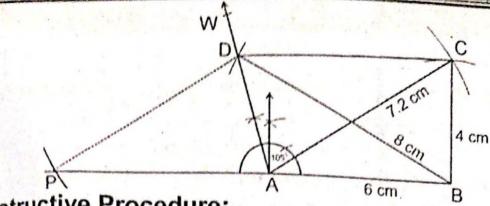
$$0 = 0$$

Thus, solution set = $\left\{\frac{17}{4}\right\}$ Checked.

(b) Construct a triangle equal in area to quadrilateral ABCD, having: the (4)

 $\overrightarrow{\text{mAB}} = 6 \text{ cm}, \ \overrightarrow{\text{mBC}} = 4 \text{ cm}, \ \overrightarrow{\text{mAC}} = 7.2 \text{ cm}$

m∠BAD = 105° and mBD = 8 cm Ans



Constructive Procedure:

- (i) Take a line segment AB = 6 cm.
- (ii) Take an angle ∠BAW = 105° at point A.
- (iii) Take B as centre and draw an arc of radius 8 cm which cuts AW at D.
- (iv) Take A and B as centre and draw arcs of radius 7.2 cm and 4 cm, respectively. These intersect at point C.
- (v) Join C to B and D.
- (vi) Join C to A.
- (vii) Take CP II CA which meets BA extended at P.

 ABCD is the required quadrilateral. While, CPB is the required triangle which is equal to quadrilateral ABCD.
- Q.9. Prove that the right bisectors of the sides of a triangle are concurrent. (9)
- For Answer see Paper 2014 (Group-I), Q.9.

OR

Prove that triangles on the same base and of the same altitudes are equal in area.

For Answer see Paper 2014 (Group-I), Q.9(OR).